# Efficient Sequential Algorithms, Comp309

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2010–2011 Module Organiser, Igor Potapov Supplementary Material: String Algorithms.

# Lempel-Ziv Welch (LZW) Compression

We will now look at the Lempel-Ziv Welch compression algorithm, which is a lossless compression algorithm that does particularly well on data with repetitions.

A useful feature of LZW compression is that the dictionary is built adaptively during encoding. The dictionary does not need to be passed with the compressed text — the decoding algorithm produces the same dictionary from the compressed text.

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A useful feature of LZW compression is that the dictionary is built adaptively during encoding. The dictionary does not need to be passed with the compressed text — the decoding algorithm produces the same dictionary from the compressed text. The original paper that describes the LZW algorithm is:

Terry A. Welch. A Technique for High Performance Data Compression. IEEE Computer, Vol. 17, No. 6, 1984, pp. 8-19.

This paper describes an improvement to a compression method introduced by Ziv and Lempel in 1977 and 1978.

LZW and variants have been used in popular software such as Unix compress and GIF compression.

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### Sources

# There is a lot of information about LZW on the web. See, for example, Wikipedia, or the nice animation at

http://www.data-compression.com/lempelziv.shtml

Also, see Dave Marshall's notes.

http://www.cs.cf.ac.uk/Dave/Multimedia

# Compression

The dictionary is initialised so that there is a codeword for every extended ASCII character.

\_

character	code word
null	0
А	65
В	66
С	67
D	68
	255

# The compression algorithm

```
Initialise dictionary
w \leftarrow \text{NIL}
while there is a character to read
       k \leftarrow next character in text
       If wk is in the dictionary
              w \leftarrow wk
       Else
             Add wk to the dictionary
             Output the code for w
              w \leftarrow k
Output the code for w
```

#### T = ABACABA

[ ]	[ ]		dictionary		[]	
	í I					Initialise dictionary
	í I		A	65		$w \leftarrow \text{NIL}$
	í I		В	66		while there is a char to read
	í I	rest of	C	67		$k \leftarrow$ next char in text
w	k	text				If <i>wk</i> is in the dictionary
NIL	A	BACABA		( I	output	$w \leftarrow wk$
A	В	ACABA	AB	256	65	Else
В	A	CABA	BA	257	66	Add wk to dictionary
Α	C	ABA	AC	258	65	Output code for w
C	A	BA	CA	259	67	$w \leftarrow k$
A	В	A		( !		Output the code for w
AB	A		ABA	260	256	
Α					65	

# The Decompression Algorithm

The basic decompression algorithm is as follows.

Initialise dictionary  $c \leftarrow \text{first codeword}$ output the translation of c  $W \leftarrow C$ While there is a codeword to read  $c \leftarrow \text{next codeword}$ output the translation of c  $s \leftarrow$  translation of w  $k \leftarrow$  first character of translation of c Add *sk* to dictionary  $W \leftarrow C$ 

#### Code = 65,66,65,67,256,65

l l	,			dictio	nary		
				A B C	 65 66 67		Initialise dictionary $c \leftarrow$ first codeword output the translation of $c$
C	W	S	k			output	$w \leftarrow c$ While there is a codeword
65 66	65	A	в			A B	to read
	66			AB	256		$c \leftarrow$ next codeword output the translation of $c$
65	65	В	Α	BA	257	A	$s \leftarrow$ translation of $w$
67		A	С			С	$k \leftarrow \text{first character of}$ translation of <i>c</i>
256	67	С	А	AC	258	AB	Add <i>sk</i> to dictionary
200	256			CA	259		$w \leftarrow c$
65	1 '	AB	Α			A	
	65			ABA	260		

## Refinement

The decoding algorithm as stated does not always work as it fails if c is not in the dictionary.

		dictio		
		 A	 65	
		В	66	
		С	67	
W	k			
NIL	Α			output
A	В	AB	256	65
В	С	BC	257	66
С	Α	CA	258	67
Α	В			
AB	Α	ABA	259	256
Α	В			
AB	Α			
ABA				259

Initialise dictionary  $w \leftarrow \text{NIL}$ while there is a char to read  $k \leftarrow$  next char in text If *wk* is in the dictionary  $w \leftarrow wk$ Else Add *wk* to dictionary Output code for w  $w \leftarrow k$ Output the code for w

Code = 65,66,67,256,259

				dictionary			Initialise dictionary
							$c \leftarrow first codeword$
				Α	65		output the translation of <i>c</i>
				В	66		$w \leftarrow c$
				С	67		While there is a codeword
С	w	S	k			output	to read
65	65					Á	$c \leftarrow next  codeword$
66		А	В			В	output the translation of <i>c</i>
	66			AB	256		$s \leftarrow \text{translation of } w$
67		В	С			С	$k \leftarrow \text{first character of}$
	67			BC	257		translation of <i>c</i>
256		С	A			AB	Add sk to dictionary
	256			CA	258		$w \leftarrow c$
259						?	

# The problem arises when the dictionary has *cs* in the dictionary for a character *c* and a string *s* and then the input contains *cscsc*.

The decompression algorithm can be modified to deal with this case.

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The decompression algorithm can be modified to deal with this case.

```
Initialise dictionary
c \leftarrow \text{first codeword}
output the translation of c
W \leftarrow C
While there is a codeword to read
       c \leftarrow \text{next codeword}
       s \leftarrow translation of w
       If c is in dictionary
              k \leftarrow first character of translation of c
              output the translation of c
       Else (* c is the code for what we add here*)
              k \leftarrow first character of s
              output sk
       Add sk to dictionary
       w \leftarrow c
```

Code = 65,66,67,256,259

				dictionary		-	Initialise dictionary $c \leftarrow \text{first codeword}$
				 A	 65	ĺ	output the translation of <i>c</i>
				B	66		$w \leftarrow c$ While there is a codeword
с	w	s	k	С	67	output	$\textit{c} \leftarrow next  codeword$
65	65	3	n.	•••		A	$s \leftarrow \text{translation of } w$
66		A	В			B	If <i>c</i> is in dictionary $k \leftarrow 1$ st char of trans <i>c</i>
	66			AB	256		output trans $c$
67	67	В	С	BC	257	С	Else (* <i>c</i> is next added*)
256	07	С	Α		201	AB	$k \leftarrow \text{first character of } s$
	256			CA	258		output <i>sk</i> Add <i>sk</i> to dictionary
259		AB	Α			ABA	$W \leftarrow C$
	259			ABA	259		

There are lots of interesting implementation issues. For example, what if the dictionary runs out of space?

Also, if we start re-using dictionary space, what data structure do we use to make dictionary access efficient?

GIF compression solves the problem of dictionary overflow by having variable-length codes. We will not cover the details.